

# EC1340-Fall 2023

## Problem Set 1

(Updated 18 August 2023)

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When you write up your answers, your goals should be to (1) be correct, and (2) convince your reader that your answer is correct. It is always helpful if your work is legible and if all steps are presented, possibly with a line of explanation.

In the case of empirical exercises, your goal should be to provide enough information to allow a reader to replicate your answer. This requires a description of data and data sources as well as a description of your analysis of the data.

Answers which do not achieve these goals will not be awarded full credit.

### Problems

1. Consider the BDICE model introduced in class,

$$\begin{aligned} \max_{s, M} u(c_1, c_2) \\ \text{s.t. } W = c_1 + s + M \end{aligned} \tag{1}$$

$$c_2 = (1 + r)s - \gamma(T_2 - T_1)s$$

$$E = (1 - \rho_4 \frac{M}{W})(\rho_5(c_1 + s)) \tag{2}$$

$$P_2 = \rho_0 E + P_1 \tag{3}$$

$$T_2 = \rho_1(P_2 - P_1) + T_1 \tag{4}$$

- (a) Use the numbered constraints to write the change in climate,  $T_2 - T_1$ , in terms of  $W$  and  $M$ .
  - (b) Using the expression you just found, together with the values of  $W, \rho_0, \rho_1$  and  $\rho_5$  given in lecture to calculate the change in temperature we should expect from production of  $W$  today. For the purposes of this calculation, let  $P_1 = 400$  and suppose that zero resources are devoted to mitigation. (Hint: the trick here is to get the units to be consistent for all of the quantities involved).
  - (c) Consider a program of technology transfer from the developed world to the developing world that simultaneously (1) doubled world output, and (2) reduced  $\rho_5$  to US levels, about one third of the world average level. What would be the resulting counterfactual climate change?
  - (d) You have just used the BDICE model to predict climate change under two hypothetical scenarios. How do these scenarios compare to the various RCPs that the IPCC 2013 report presents. Can you say anything about how well the BDICE model matches IPCC predictions?
2. These questions ask you to do some elementary calculations to relate the weight of fuel, emissions,  $CO_2$  concentrations and climate change. You will probably need to refer to numbers given in lecture.

- (a) From Hansen figure 22, estimate the change in atmospheric  $CO_2$  concentrations that would result from burning all coal reserves.
  - (b) Using Nordhaus' rule of thumb for the relationship between atmospheric  $CO_2$  and climate change, estimate the change in world average temperature in 100 years that would result from burning the world's coal supply tomorrow.
  - (c) Using figure 25 in Hansen, estimate how much coal we will burn over the next 100 years if the rate of consumption stays constant at about 2010 levels.
  - (d) Again using Nordhaus' rule of thumb, what is the likely impact on climate in 100 years of this consumption of coal? (To do this calculation, you can suppose that the impact on climate in 2111 of emissions in 2011 is the same as for emissions in 2110.)
3. In table 2 of their paper 'Climate Change, Mortality, and Adaptation: Evidence from Annual Fluctuations in Weather in the U.S.', (at <http://www.jstor.org/stable/41288654> ), O. Deschenes and M. Greenstone find that an increase of daily average temperature of about 4 degrees Fahrenheit causes about 6 extra deaths per day in the United States. Suppose that in 100 years, the rest of the world's death rate responds to changes in climate in just the same way as does the US today. Also suppose that the world population and US population are the same as they are today.
- Use this information, together with the discussion from lecture, to calculate the increase in the daily death rate in 100 years that results from burning one 50 liter tank of gasoline.
4. We will end up talking a lot about carbon taxes. This question asks you figure out the relationship between a carbon tax and a gasoline tax.
- (a) Consider tax rates of 20\$, 50\$, 100\$, and 200\$. If this tax is levied on  $c$ , what are the corresponding implied taxes on a gallon of gasoline? What if the tax is levied on  $CO_2$ ? Explain your reasoning and write your results as a table.
  - (b) Gasoline prices in Italy in 2023 are about 1.87EU/litre. At 3.8 litres per gallon and  $1EU = 1.1USD$ , this is about 7.80 USD per gallon. Gasoline prices in the US in 2023 are about 3.5 USD per gallon. How big a tax on  $CO_2$  is required to make up the difference?

For the purposes of this problem, the following data may be helpful. Gasoline is about 87% carbon by weight and each gallon weighs about 6.7 pounds. Carbon taxes are usually stated in terms of metric tons. A metric ton is 1000kg or about 2200 pounds (vs. short ton which is 2000 pounds)

5. (Carbon taxes cont'd) This question asks you figure out the impact of a carbon tax on a typical utility bill. An average household in Rhode Island uses about 500 KwH/month of electricity. How much tax would an average household pay under a 100 and 200\$/ton tax on  $CO_2$  if their power is produced in a gas fired power plant?